

國立高雄大學 101 學年度研究所碩士班招生考試試題

科目：工程數學  
考試時間：100 分鐘

系所：應用物理學系  
本科原始成績：100 分

是否使用計算機：是

每題 10 分

1.  $y(x)'' + y(x)' \sin [y(x)] = 0$  請問  $y(x)$ ?

2.  $y(x)'' + 4y(x)' + 5y(x) = 0$  初始條件  $y(0) = 2, y(0)' = -5$

求  $y(x)$ ?

3.  $y(t) + \int_0^t (t - \tau)y(\tau)d\tau = 1$  求  $y(t)$

4.  $A = \begin{bmatrix} 3 & -1 & 1 \\ -15 & 6 & -5 \\ 5 & -2 & 2 \end{bmatrix}$  求  $A^{-1}$

5. 求  $\begin{bmatrix} 1 & 0 & 1 \\ 0 & 3 & 2 \\ 0 & 0 & 2 \end{bmatrix}$  eigenvalues 與 eigenvectors

6. 求平面積分  $\iint_S (\nabla \times F) \cdot n dA$ , 函數

$F = [-e^y, e^z, e^x]$ , 平面  $S: z = x + y$  ( $0 \leq x \leq 1, 0 \leq y \leq 1$ )

7. 求週期函數  $f(x) = |x|$  ( $-1 < x < 1$ ) 的 Fourier 級數

8. 求複數積分  $\oint_C \frac{dz}{z^2 - 1}$ ,  $C: |z + 1| = 1$

9. 求積分  $\int_0^{2\pi} \frac{d\theta}{37 - 12 \cos \theta}$

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10. 求積分  $\int_{-\infty}^{\infty} \frac{x+5}{x^3-x} dx$

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科目：電子學  
 考試時間：100 分鐘

系所：應用物理學系  
 本科原始成績：100 分

是否使用計算機：是

- The reverse-saturation current of a silicon pn junction diode at  $T = 300 \text{ K}$  is  $I_s = 10^{-12} \text{ A}$ . Determine the temperature range over which  $I_s$  varies from  $2 \times 10^{-12} \text{ A}$  to  $60 \times 10^{-12} \text{ A}$ . (20%)
- With the circuit in Fig. 1, let  $\beta = 100$ . (a) Find  $R_{TH}$  and  $V_{TH}$  for the base circuit. (10%) (b) Determine  $I_{CQ}$ ,  $V_{CEQ}$ . (10%)
- If the emitter voltage ( $V_E$ ) of the circuit shown in Fig. 2 is 1 V, assume that  $|V_{BE}| = 0.7 \text{ V}$ , what are  $V_B$ ,  $I_B$ ,  $I_E$ ,  $I_C$ ,  $V_C$ ,  $\beta$  and  $\alpha$ ? (20%)
- Determine the deviation from the ideal due to a finite differential gain. Consider an inverting op-amp with  $R_1 = 10 \text{ k}\Omega$  and  $R_2 = 100 \text{ k}\Omega$  in Fig. 3. Determine the closed-loop gain for:  $A_{od} = 10^2$ ,  $10^3$ ,  $10^4$ ,  $10^5$  and  $10^6$ . Calculate the percent deviation from the ideal gain. (20%)
- Determine the corner frequencies and limiting horizontal asymptotes of a common-emitter circuit with an emitter bypass capacitor. Consider the circuit in Fig. 4 with parameters  $R_E = 4 \text{ k}\Omega$ ,  $R_C = 2 \text{ k}\Omega$ ,  $R_S = 0.5 \text{ k}\Omega$ ,  $C_E = 1 \mu\text{F}$ ,  $V^+ = 5 \text{ V}$ , and  $V^- = -5 \text{ V}$ . The transistor parameters are:  $\beta = 100$ ,  $V_{BE(on)} = 0.7 \text{ V}$ , and  $r_o = \infty$ . (20%)

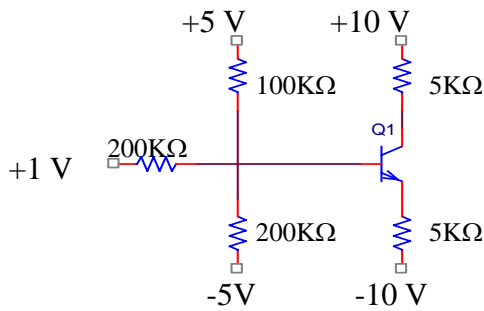


Fig. 1

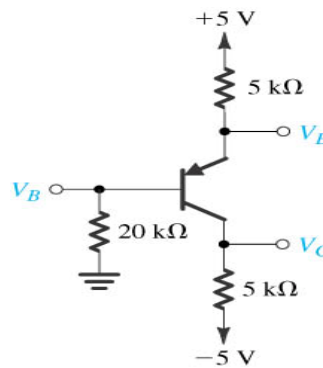


Fig. 2

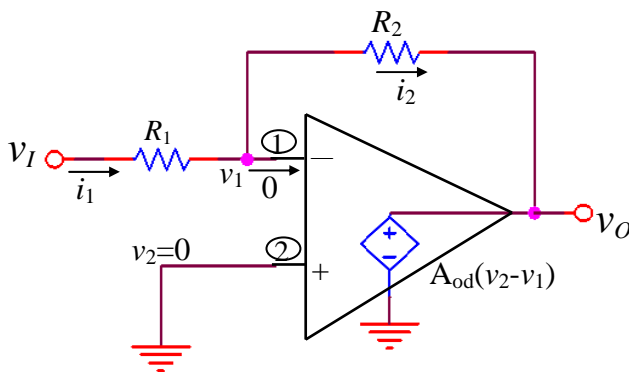


Fig. 3

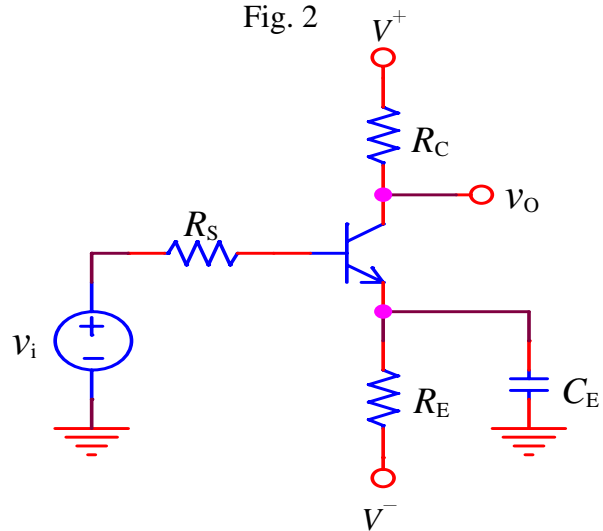


Fig. 4

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1. Write down the Maxwell's equations in matter and boundary conductions. (10%)
2. Two point charges,  $3q$  and  $-q$ , are separated by a distance  $a$ , as shown in Fig. 1. Find (a) the monopole moment, (b) the dipole moment, and (c) the approximate potential at a large distance. (15%)

3. A constant potential  $V_0$  is specified on the surface of a hollow sphere, of radius  $R$ . Find the potential inside and outside the sphere. (20%)

4. A uniformly magnetized sphere with  $\vec{M} = M\hat{z}$ , as shown in Fig. 2. Find the (a) bound volume current, (b) bound surface current, (c) magnetic field,  $\vec{B}$ , inside the sphere and (d)  $\vec{H}$ . (note that

$$\vec{H} \equiv \frac{\vec{B}}{\mu_0} - \vec{M} ) (20\%)$$

5. A long coaxial cable carries current  $I$  (The current flows down the surface of the inner cylinder, radius  $a$ , and back along the outer cylinder, radius  $b$ . Two cylinders are held at potential difference  $V$ ), Fig. 3. Calculate (a) the electric field and (b) the magnetic field between the cylinders. Find (c) the magnetic energy stored in and (d) the self-inductance of a section of length  $l$ . Calculate (e) the Poynting vector and (f) the power transported down the coaxial cable and (g) the electromagnetic momentum stored in the fields in a section of length  $l$ . (35%)

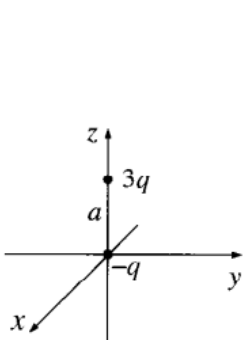


Fig. 1

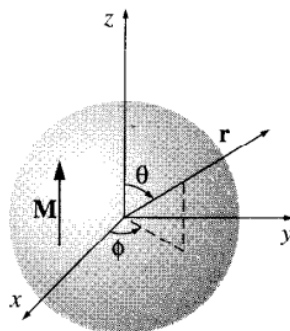


Fig. 2

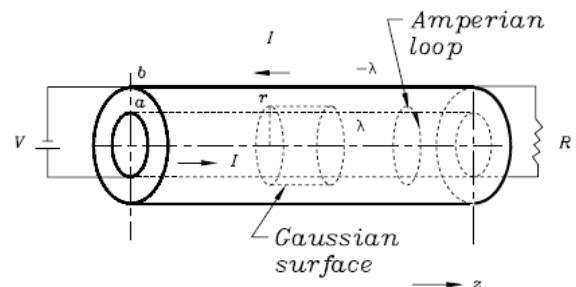


Fig. 3